Erratum: Kinetic theory of spin transport in n-type semiconductor quantum wells [J. Appl. Phys. 93, 410 (2003)]

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There are some misprints in the text of our paper [JAP **93**, 410 (2003)]. They are corrected as following. The Poisson equation (5) in the paper should be

$$\nabla_{\mathbf{r}}^2 \Psi(\mathbf{r}, t) = e[n(\mathbf{r}, t) - n_0(\mathbf{r})]/\varepsilon_0, \tag{5}$$

The screen constant κ in the Eq. (8) should be $\kappa^2 = 6\pi n_0(\mathbf{r})e^2/(aE_f)$. There are some misprints in Eqs. (9)-(12), the corrected equations are

$$\frac{\partial f_{\sigma}(\mathbf{R}, \mathbf{k}, t)}{\partial t} \bigg|_{\sigma} = 2 \text{Im}[\bar{\varepsilon}_{\sigma - \sigma}(\mathbf{R}, \mathbf{k}, t) \rho_{-\sigma \sigma}(\mathbf{R}, \mathbf{k}, t)]$$
(9)

$$\frac{\partial \rho_{\sigma-\sigma}(\mathbf{R}, \mathbf{k}, t)}{\partial t} \bigg|_{c} = -i[\bar{\varepsilon}_{\sigma\sigma}(\mathbf{R}, \mathbf{k}, t) - \bar{\varepsilon}_{-\sigma-\sigma}(\mathbf{R}, \mathbf{k}, t)]\rho_{\sigma-\sigma}(\mathbf{R}, \mathbf{k}, t) - i\bar{\varepsilon}_{\sigma-\sigma}(\mathbf{R}, \mathbf{k}, t)[f_{-\sigma}(\mathbf{R}, \mathbf{k}, t) - f_{\sigma}(\mathbf{R}, \mathbf{k}, t)]$$
(10)

$$\frac{\partial f_{\sigma}(\mathbf{R}, \mathbf{k}, t)}{\partial t} \Big|_{s} = \left\{ -2\pi \sum_{\mathbf{q}q_{z}\lambda} |g_{\mathbf{q}q_{z}\lambda}|^{2} \delta(\varepsilon_{\mathbf{k}} - \varepsilon_{\mathbf{k}-\mathbf{q}} - \Omega_{\mathbf{q}q_{z}\lambda}) \Big[N_{\mathbf{q}q_{z}\lambda} \Big(f_{\sigma}(\mathbf{R}, \mathbf{k}, t) - f_{\sigma}(\mathbf{R}, \mathbf{k} - \mathbf{q}, t) \Big) \right. \\
+ f_{\sigma}(\mathbf{R}, \mathbf{k}, t) \Big(1 - f_{\sigma}(\mathbf{R}, \mathbf{k} - \mathbf{q}, t) \Big) - \operatorname{Re} \Big(\rho_{\sigma-\sigma}(\mathbf{R}, \mathbf{k}, t) \rho_{\sigma-\sigma}^{*}(\mathbf{R}, \mathbf{k} - \mathbf{q}, t) \Big) \Big] \\
- 2\pi N_{i} \sum_{\mathbf{q}} U_{\mathbf{q}}^{2} \delta(\varepsilon_{\mathbf{k}} - \varepsilon_{\mathbf{k}-\mathbf{q}}) \Big[f_{\sigma}(\mathbf{R}, \mathbf{k}, t) \Big(1 - f_{\sigma}(\mathbf{R}, \mathbf{k} - \mathbf{q}, t) \Big) - \operatorname{Re} \Big(\rho_{\sigma-\sigma}(\mathbf{R}, \mathbf{k}, t) \Big) \\
\times \rho_{\sigma-\sigma}^{*}(\mathbf{R}, \mathbf{k} - \mathbf{q}, t) \Big) \Big] - 2\pi \sum_{\mathbf{k}' \mathbf{q} \sigma'} V_{\mathbf{q}}^{2} \delta(\varepsilon_{\mathbf{k}-\mathbf{q}} - \varepsilon_{\mathbf{k}} + \varepsilon_{\mathbf{k}'} - \varepsilon_{\mathbf{k}'-\mathbf{q}}) \\
\times \Big[\Big(1 - f_{\sigma}(\mathbf{R}, \mathbf{k} - \mathbf{q}, t) \Big) f_{\sigma}(\mathbf{R}, \mathbf{k}, t) \Big(1 - f_{\sigma'}(\mathbf{R}, \mathbf{k}', t) \Big) f_{\sigma'}(\mathbf{R}, \mathbf{k}' - \mathbf{q}, t) \\
+ \frac{1}{2} \operatorname{Re} \Big(\rho_{\sigma-\sigma}(\mathbf{R}, \mathbf{k} - \mathbf{q}, t) \rho_{-\sigma\sigma}(\mathbf{R}, \mathbf{k}, t) \Big) \Big(f_{\sigma'}(\mathbf{R}, \mathbf{k}', t) - f_{\sigma'}(\mathbf{R}, \mathbf{k}' - \mathbf{q}, t) \Big) \Big] \Big\} \\
- \Big\{ \mathbf{k} \leftrightarrow \mathbf{k} - \mathbf{q}, \mathbf{k}' \leftrightarrow \mathbf{k}' - \mathbf{q} \Big\} \tag{11}$$

and

$$\begin{split} &\frac{\partial \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t)}{\partial t}\bigg|_{s} \\ &= \Bigg\{-\pi \sum_{\mathbf{q}q_{z}\lambda} g_{\mathbf{q}q_{z}\lambda}^{2} \delta(\varepsilon_{\mathbf{k}} - \varepsilon_{\mathbf{k}-\mathbf{q}} - \Omega_{\mathbf{q}q_{z}\lambda}) \Big[\Big(f_{\sigma}(\mathbf{R},\mathbf{k},t) + f_{-\sigma}(\mathbf{R},\mathbf{k},t)\Big) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \\ &+ \Big(f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) + f_{-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) - 2\Big) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) - 2N_{\mathbf{q}q_{z}\lambda} \Big(\rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) - \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t)\Big) \Big] \\ &- \pi N_{i} \sum_{\mathbf{q}\lambda} U_{\mathbf{q}}^{2} \delta(\varepsilon_{\mathbf{k}} - \varepsilon_{\mathbf{k}-\mathbf{q}}) \Big[\Big(f_{\sigma}(\mathbf{R},\mathbf{k},t) + f_{-\sigma}(\mathbf{R},\mathbf{k},t)\Big) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \\ &- \Big(2 - f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) - f_{-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t)\Big) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \\ &- \pi \sum_{\mathbf{k}'\mathbf{q}\sigma'} V_{\mathbf{q}}^{2} \pi \delta(\varepsilon_{\mathbf{k}-\mathbf{q}} - \varepsilon_{\mathbf{k}} + \varepsilon_{\mathbf{k}'} - \varepsilon_{\mathbf{k}'-\mathbf{q}}) \Big\{ \Big[f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) + \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) f_{-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big\} \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) + \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) f_{-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) + \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) f_{-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) + \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) f_{-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) + \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) f_{-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) + \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) f_{-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) + \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) f_{-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) + \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) f_{-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) + \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) f_{-\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) f_{-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k}-\mathbf{q},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) + \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k},t) \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) + \rho_{\sigma-\sigma}(\mathbf{R},\mathbf{k},t) \Big] \Big] \Big[\Big[f_{\sigma}(\mathbf{R},\mathbf{k$$

$$\times \left[f_{\sigma'}(\mathbf{R}, \mathbf{k}', t) - f_{\sigma'}(\mathbf{R}, \mathbf{k}' - \mathbf{q}, t) \right] + \rho_{\sigma - \sigma}(\mathbf{R}, \mathbf{k}, t) \left[\left(1 - f_{\sigma'}(\mathbf{R}, \mathbf{k}', t) \right) f_{\sigma'}(\mathbf{R}, \mathbf{k}' - \mathbf{q}, t) \right] - \rho_{\sigma' - \sigma'}(\mathbf{R}, \mathbf{k}', t) \rho_{-\sigma'\sigma'}(\mathbf{R}, \mathbf{k}' - \mathbf{q}, t) \right] - \rho_{\sigma - \sigma}(\mathbf{R}, \mathbf{k} - \mathbf{q}, t) \left[f_{\sigma'}(\mathbf{R}, \mathbf{k}', t) \left(1 - f_{\sigma'}(\mathbf{R}, \mathbf{k}' - \mathbf{q}, t) \right) \right] - \rho_{\sigma' - \sigma'}(\mathbf{R}, \mathbf{k}', t) \rho_{-\sigma'\sigma'}(\mathbf{R}, \mathbf{k}' - \mathbf{q}, t) \right] \right\} - \left\{ \mathbf{k} \leftrightarrow \mathbf{k} - \mathbf{q}, \mathbf{k}' \leftrightarrow \mathbf{k}' - \mathbf{q} \right\}$$

$$(12)$$

respectively.

The numerical results in the paper are based on the correct formulas.